

C3 Composite Functions

$$f(x) = \frac{x^2-4}{3}, \quad x \leq 0$$

$$g(x) = \ln|3x - 1|$$

Solve $gf(x) = 0$

$$gf(x) = \ln|x^2 - 5|, \quad x \leq 0$$

$$\ln|x^2 - 5| = 0 \Rightarrow |x^2 - 5| = 1$$

$$\text{Either } x^2 - 5 = 1 \text{ or } 5 - x^2 = 1$$

In the first case $x^2 = 6$ and in the second case $x^2 = 4$.

Since $gf(x)$ is defined for $x \leq 0$ the negative square root is required in each case.

$$x = -\sqrt{6} \text{ or } x = -2.$$