## A GCSE Maths Question

The radius of the smaller circle is 3 cm . The radius of the larger circle is 6 cm . The circles touch at a point. The tangent to the smaller circle, shown in the diagram, passes through the centre, $D$, of the larger circle.


Find the area shaded.


$$
\begin{gathered}
A B=3 \text { and } B D=3+6 \text { so by Pythagoras' theorem } A D^{2}+3^{2}=9^{2} \\
A D=6 \sqrt{2} \\
A E=\frac{1}{3} A D=2 \sqrt{2}
\end{gathered}
$$

The required area is difference between the areas of triangle $B C D$ and triangle $B C F$.

$$
\text { Shaded area }=\frac{B C \times A D}{2}-\frac{B C \times A E}{2}=\frac{3 \times 6 \sqrt{2}}{2}-\frac{3 \times 2 \sqrt{2}}{2}=6 \sqrt{2} \mathrm{~cm}^{2}
$$

